

On some identities involving k -Jacobsthal numbers

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Resumo

In recent article, Jhala, Sisodiya and Rathore [2] proved a number of sum identities involving a k -Jacobsthal Numbers $J(k, n)$ defined by $J(k, n + 1) = kJ(k, n) + 2J(k, n - 1)$; for $n \geq 1$, with initial condition $J(k, 0) = 0$, $J(k, 1) = 1$. For $n \geq 1$, we have that $J(1, n) = J_n$, the n th Jacobsthal number. For example, Jhala, Sisodiya and Rathore proved the following identities using Binet's formula for the general term of the k -Jacobsthal sequence, for all integers $n \geq 0$:

Theorem 1. (*Catalan's identity*)

$$J(k, n - r)J(k, n + r) - J^2(k, n) = (-1)^{n+1-r} J^2(k, r) 2^{n-r}.$$

Theorem 2. (*D'ocagne's identity*) If $m > n$ then $J(k, m)J(k, n + 1) - J(k, m + 1)J(k, n) = (-2)^n J(k, m - n)$.

Many authors have employed the technique of counting via tilings in different contexts, like in [1]. Our goal in this work is to view above identities combinatorially with point view generalized, providing bijective arguments from the context of tilings as discussed in [1].

Referências

- [1] Benjamim, A. T. and Quinn, J. J. Proofs that Really Count: *The Art of Combinatorial Proof*. The Dolciani Mathematical Expositions, 27, Mathematical Association of America, Washington, DC, 2003.
- [2] Jhala D., Sisodiya, K., Rathore, G.P.S, *On Some Identities for k -Jacobsthal Numbers*, Int. Journal of Math Analysis, Vol. 7, 2013, no. 12, 551-556.